李瑩英： 幾何分析討論班(I) (II)

Nature of the course 加開選修		Area： ■幾何與拓樸			
Course number		Section number	免填	Number of credits	3
Course title	課程名稱：幾何分析討論班(I) (II)				
Instructor	教授： 李瑩英				
開設學期： ■上學期　　■下學期		上課時間： 星期三，五 節次1:30-2:45		開課對象： ■研究生	

I.　　＊Contents：

In this course, we will study various important topics in Geometric Analysis which include minimal submanifolds, harmonic maps, Lagrangian mean curvature flow, general relativity, spectral theory, and etc. Each student in the class needs to pick a direction and study related material and papers. Then discuss with the instructor and present in turn.

II.　　Course prerequisite：

　　Graduate school differential geometry

III.　　＊Reference material（textbook(s)）：

　　Assign each student his/her own list of papers in the beginning and middle of the class

IV.　　＊Grading scheme：請填寫各項計分之百分比，例如：期中30% 期末40% 作業10% 報告20%，總計100%

　　In class presentations and discussions 100%

V.　　＊Course Goal：

　　Be familiar with some important results and direction in the field of Geometric Analysis.

　　And try to work on a research problem from the study.

　　Also practice presentations in a group.

崔 茂 培 ： 幾 何 分 析 專 題

Nature of the course 加開選修		Area： 分析，幾何與拓樸			
Course number		Section number	免填	Number of credits	3
Course title	課程名稱：幾何分析專題 Topics in Geometric Analysis				
Instructor	教授： Mao-Pei Tsui				
開設學期： 全學年		上課時間： 星期　　節次		開課對象： 皆可	

I.　　＊**Contents**：Geometric evolution equations have seen tremendous progress in the last 30 years. In 1964 the seminar paper of Eells and Sampson introduced the harmonic heat flow and used it to prove the existence of harmonic maps into targets with non-positive sectional curvature. The year 1982 marked the beginning of Ricci flow with the appearance of Hamilton's paper on 3-manifolds with positive Ricci curvature. In 1984, Gerhard Huiken studied the mean curvature flow of convex hypersurfaces. The main topics of this course are the interaction between nonlinear partial differential equations and differential geometry, especially in areas where the deformation of geometric objects by nonlinear parabolic equations can bring a new understanding to the geometric problems. Such connections show up in Hamilton-Perelman's proof of Poincare and Thurston's geometrization conjecture via Ricci flow; as well as in Huisken and Ilmanen's proof of the Riemannian Penrose conjecture via inverse mean curvature flow.

We will cover the following topics.

(1) The basic backgrounds and techniques to study geometric evolution equations

(2) Go over the fundamental papers in harmonic heat flow, Ricci flow and mean curvature flow

(3) Understanding of the long time existence and singularity analysis of various geometric evolution equations

II.　　**Course prerequisite**：

III.　　＊**Reference material（textbook(s)）**：

Book: Hamilton's Ricci Flow by Bennett Chow, Peng Lu , and Lei Ni

Papers:

1. Huisken, Gerhard. Flow by mean curvature of convex surfaces into spheres. Journal of Differential Geometry 20 (1984), no. 1, 237--266

2. Hamilton, Richard S. Three-manifolds with positive Ricci curvature. Journal of Differential Geometry 17 (1982), no. 2, 255--306.